

**MODUL PENINGKATAN PRESTASI TINGKATAN 5  
TAHUN 2024**

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# **MATEMATIK TAMBAHAN**

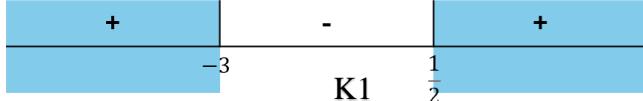
## **KERTAS 1**

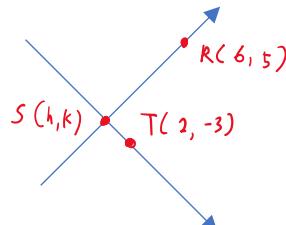
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### **PERATURAN PEMARKAHAN**

Peraturan Pemarkahan ini mengandungi **14** halaman bercetak

NO	PENYELESAIAN	SUB	JUMLAH
1	$\log_3(x-2) - \log_3 2 = \log_3 x^2 - \log_3(3x+4)$ $\log_3\left(\frac{x-2}{2}\right) = \log_3\left(\frac{x^2}{3x+4}\right)$ $\frac{x-2}{2} = \frac{x^2}{3x+4}$ $(x-2)(3x+4) = 2x^2$ $x^2 - 2x - 8 = 0$ $(x-4)(x+2) = 0$ $x = 4, x = -2$ [diabaikan]	K1 [Guna rumus log] K1 K1 [ $x^2 - 2x - 8$ dilihat] N1	4 4

NO	PENYELESAIAN	SUB	JUMLAH
2 a)	$2x^2 + 5x - 3 \geq 0$ $(2x-1)(x+3) \geq 0$ K1  <i>Titik ujian = -4</i> $(2(-4)-1)(-4+3)$ $9 \geq 0$ <i>Titik ujian = 0</i>  $-3 < 0$ <i>Titik ujian = 1</i> $(2(1)-1)(1+3)$ $4 \geq 0$  Julat nilai $x$ ialah $x \leq -3$ atau $x \geq \frac{1}{2}$	3	6
2 b)	$f(x) = 2(x^2 - 6x + 5)$ $= 2\left[x^2 - 6x + \left(-\frac{6}{2}\right)^2 - \left(-\frac{6}{2}\right)^2 + 5\right]$ $= 2(x-3)^2 - 8$ <i>Titik minimum = (3, -8)</i> Persamaan paksi simetri, $x = 3$ N1  Nota: Tidak terima (i) $\frac{f(x)}{2}$ dan $x-3=0$	3	

NO	PENYELESAIAN	SUB	JUMLAH
3	$M_{RS} = \frac{5-k}{6-h}$ $M_{ST} = \frac{k-(-3)}{h-2}$ $\left(\frac{5-k}{6-h}\right)\left(\frac{k-(-3)}{h-2}\right) = -1$ $\frac{5k+15-k^2-3k}{6h-12-h^2+2h} = -1$ $-k^2+2k+15 = -(-h^2+8h-12)$ $h^2+k^2-8h-2k-3=0$ <p style="color:red;">K1 K1 K1 N1 [semua langkah betul]</p> 	4	4

NO	PENYELESAIAN	SUB	JUMLAH
4 a) (i)	0	N1	5
4 a) (ii)	$x = -\frac{\pi}{2}; x = -\frac{3}{2}\pi$	N1 [dilihat]	
4 b) (i)	$y = - \tan x $	N1	
4 b) (ii)	$-2\pi \leq x \leq 0$	N1 [terima $-\frac{5}{2}\pi \leq x \leq 0$ ]	
4 b) (iii)	$y \leq 0$	N1	

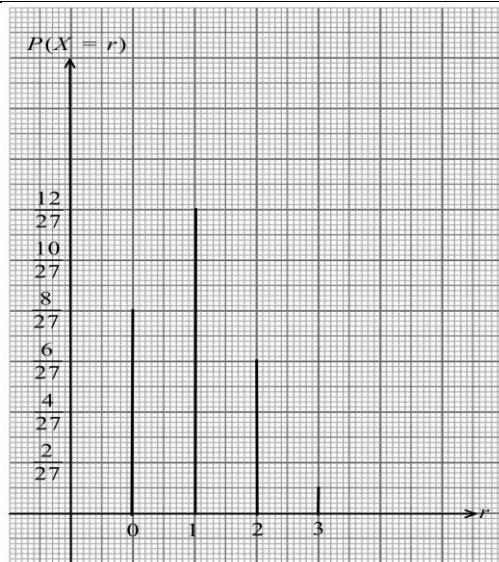
NO	PENYELESAIAN	SUB	JUMLAH
5 a)	Panjang lengkok AC = $100 - 30 - 30 = 40$ Sudut minor AOC: $40 = 30 \times \theta$ $\theta = 1.333 \text{ rad} @ \frac{4}{3} \text{ rad} @ 1\frac{1}{3} \text{ rad}$	K1 N1	2
5 b)	Luas sektor $OAC = \frac{1}{2} \times 30^2 \times 1.333$ $= 599.85 \text{ m}^2$ atau Luas sektor $OPR = \frac{1}{2} \times 40^2 \times 1.333$ $= 1066.4 \text{ m}^2$ Luas kawasan berlorek = $1066.40 - 599.85$ $466.55 \leftrightarrow 466.67$ $\frac{1400}{3}$	K1 N1	4

NO	PENYELESAIAN	SUB	JUMLAH
6. (a) (i)	$\begin{aligned}\overrightarrow{AC} &= \overrightarrow{AB} + \overrightarrow{BC} \\ &= \begin{pmatrix} 12 \\ 0 \end{pmatrix} + \begin{pmatrix} -4 \\ -8 \end{pmatrix} \\ &= \begin{pmatrix} 8 \\ -8 \end{pmatrix}\end{aligned}$ <span style="float: right;">P1 N1</span>	2	
6 a) (ii)	$\begin{aligned} \overrightarrow{AC}  &= \sqrt{8^2 + (-8)^2} = 8\sqrt{2} \quad \text{K1} \\ \overrightarrow{AC} &= \frac{8i - 8j}{8\sqrt{2}} = \frac{i - j}{\sqrt{2}} \\ \overrightarrow{AC} &= \begin{pmatrix} \frac{1}{\sqrt{2}} \\ -\frac{1}{\sqrt{2}} \end{pmatrix}\end{aligned}$ <span style="float: right;">N1</span>	2	4
6 b)	$\begin{aligned}\overrightarrow{EB} &= \lambda \overrightarrow{BC} \\ \overrightarrow{EO} + \overrightarrow{OB} &= \lambda \begin{pmatrix} -4 \\ -8 \end{pmatrix} \\ \begin{pmatrix} -k \\ -6 \end{pmatrix} + \begin{pmatrix} 6 \\ 2 \end{pmatrix} &= \lambda \begin{pmatrix} -4 \\ -8 \end{pmatrix} \quad \text{K1 } [\overrightarrow{EB} = \lambda \overrightarrow{BC} \text{ mesti dilihat}] \\ -4 &= \lambda(-8) \\ \lambda &= \frac{1}{2} \quad \text{N1}\end{aligned}$ $-k + 6 = \frac{1}{2}(-4)$ $k = 8 \quad \text{N1}$	3	3

NO	PENYELESAIAN	SUB	JUMLAH
7 a)	<p><b>Alternatif A</b></p> $\begin{aligned}g(x) &= f^{-1}(x) \quad \text{P1} \\ \frac{15}{2x+7} &= x \\ a &= \frac{15-7x}{2x} \\ g(x) &= \frac{15-7x}{2x}, \quad x \neq 0 \quad \text{N1 } [x \neq 0 \text{ mesti ditulis]}\end{aligned}$ <p><b>Alternatif B</b></p>	2	4

	$fg(x) = x$ $\frac{15}{2g(x)+7} = x$ $g(x) = \frac{15-7x}{2x}$ $g(x) = \frac{15-7x}{2x}, x \neq 0 \quad \text{N1 } [x \neq 0 \text{ mesti ditulis}]$	
7 b)	$\frac{15}{2x+7} = \left( \frac{15-7x}{2x} \right)^*$ $K1 * g(x) \text{ dari (a)}$ $15(2x) = (15-7x)(2x+7)$ $2x^2 + 7x - 15 = 0$ $(2x-3)(x+5) = 0$ <p>or</p> $14x^2 + 49x - 105 = 0$ $7[(2x-3)(x+5)] = 0$ $x = \frac{3}{2}, \quad x = -5 \quad \text{N1 } [(2x-3)(x+5) \text{ mesti dilihat}]$	2

NO	PENYELESAIAN	SUB	JUMLAH																				
8 a)	<table border="1"> <tr> <td><math>X</math></td><td>0</td><td>1</td><td>2</td><td>3</td></tr> <tr> <td><math>P(X=r)</math></td><td><math>\frac{8}{27}</math></td><td><math>\frac{4}{9}</math></td><td><math>\frac{2}{9}</math></td><td><math>\frac{1}{27}</math></td></tr> </table> <p>N1 betul bagi semua 4 data</p> <p>OR</p> <table border="1"> <tr> <td><math>X</math></td><td>0</td><td>1</td><td>2</td><td>3</td></tr> <tr> <td><math>P(X=r)</math></td><td>0.2963</td><td>0.4444</td><td>0.2222</td><td>0.0370</td></tr> </table> <p>Dengan syarat pembundaran betul kepada 4 titik perpuluhan</p> <p>Rujuk graf pada muka surat 7</p>	$X$	0	1	2	3	$P(X=r)$	$\frac{8}{27}$	$\frac{4}{9}$	$\frac{2}{9}$	$\frac{1}{27}$	$X$	0	1	2	3	$P(X=r)$	0.2963	0.4444	0.2222	0.0370	3	8
$X$	0	1	2	3																			
$P(X=r)$	$\frac{8}{27}$	$\frac{4}{9}$	$\frac{2}{9}$	$\frac{1}{27}$																			
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8 b)  $P((\mu - k) < X < (\mu + k)) = 0.84$

$$P\left(\frac{65-k-65}{10} < Z < \frac{65+k-65}{10}\right) = 0.84 \quad \text{P1}$$

$$P\left(-\frac{k}{10} < Z < \frac{k}{10}\right) = 0.84 \quad \text{P1 [Graf dilukis dari sini]}$$

atau

$$1 - 2P\left(Z \geq \frac{k}{10}\right) = 0.84 \quad \text{atau} \quad 0.5 - P\left(Z \geq \frac{k}{10}\right) = 0.42 \quad \text{P1}$$

$$P\left(Z \geq \frac{k}{10}\right) = 0.08$$

$$P(Z \geq 1.406) = 0.08 \quad \text{P1 [dilihat 1.406]}$$

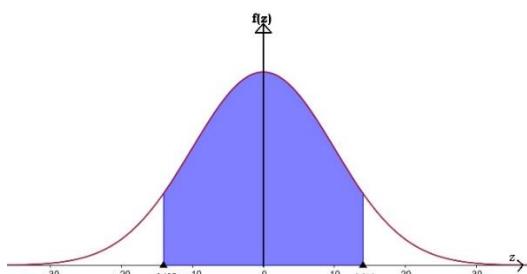
[1.406 Dibaca dari Jadual Normal Piawai]

[tidak terima jawapan dari calculator = -1.4051]

$$\frac{k}{10} = 1.406 \quad \text{K1}$$

$$k = 14.06 \quad \text{N1 [NO jika tiada lakaran graf]}$$

5



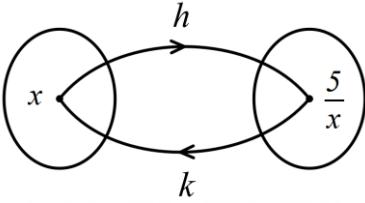
(i) Guna pembaris / alat tepi lurus

(ii)  $-\frac{k}{10}$  dan  $\frac{k}{10}$  mesti nampak

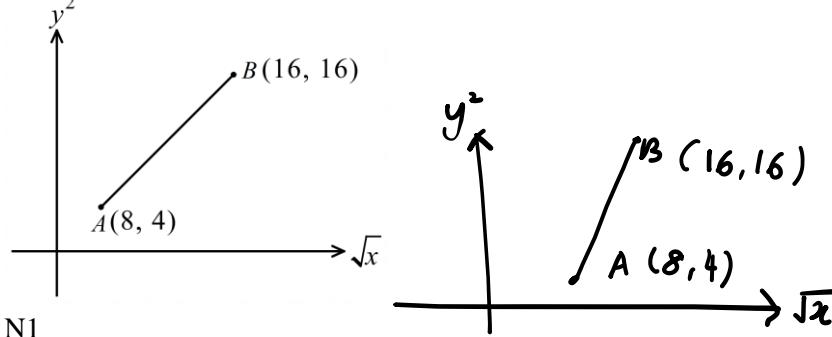
(iii) Betul label paksi  $f(z)$  dan  $z$

(iv) Lorekkan betul

NO	PENYELESAIAN	MARKAH
9. (a)	<p>had <math>\underset{x \rightarrow 0^-}{f(x)} = -1</math></p> <p>had <math>\underset{x \rightarrow 0^-}{f(x)} = 1</math></p> <p>had <math>\underset{x \rightarrow 0^-}{f(x)} \neq \underset{x \rightarrow 0^+}{\text{had } f(x)}</math>,</p> <p><math>\therefore \underset{x \rightarrow 0}{\text{had } f(x)}</math> tidak wujud</p> <p>had dari arah kiri tidak sama dengan had dari arah kanan</p>	[dilihat] 2 N1 N1
9 b)	$y = \frac{2}{x+4}$ $\delta y = f(x + \delta x) - f(x)$ $= \frac{2}{(x + \delta x) + 4} - \frac{2}{x + 4} \quad \text{K1}$ $= \frac{2(x + 4) - 2(x + \delta x + 4)}{(x + \delta x + 4)(x + 4)}$ $= \frac{-2\delta x}{(x + \delta x + 4)(x + 4)}$ $\frac{\delta y}{\delta x} = \frac{-2}{(x + \delta x + 4)(x + 4)} \quad \text{K1}$ $\frac{dy}{dx} = \underset{\delta x \rightarrow 0}{\text{had}} \frac{\delta y}{\delta x}$ $= \underset{\delta x \rightarrow 0}{\text{had}} \frac{-2}{(x + \delta x + 4)(x + 4)} \quad \text{K1 [had } \underset{\delta x \rightarrow 0}{\text{dilihat dan gantikan } \delta x = 0}\text{]}$ $= \frac{-2}{(x + 0 + 4)(x + 4)}$ $= \frac{-2}{(x + 4)(x + 4)}$ $= -\frac{2}{(x + 4)^2} \quad \text{N1}$	4
	JUMLAH	6

NO	PENYELESAIAN	SUB	JUMLAH
10 a) (i)	$h(x) = \frac{5}{x} @ k\left(\frac{5}{x}\right) = x$ $h(x) = k^{-1}(x) @ k\left(\frac{5}{x}\right) = h^{-1}\left(\frac{5}{x}\right)$ $@ h\left[k\left(\frac{5}{x}\right)\right] = k\left[h\left(\frac{5}{x}\right)\right]$ $@ hk(x) = kh(x)$ <p>* Terima jika murid guna ayat</p>	N1 N1	2
10 a) (ii)	 [meski ada anak panah dan titik]	1	6
10 b)	$gf(x) = g[2x-1]$ $= \sqrt{2x-1}$ <p>Supaya <math>gf(x)</math> tertakrif, <math>2x-1 \geq 0</math></p> $2x-1 \geq 0$ $x \geq \frac{1}{2}$ <p><b>catatan</b></p> $2x-1 > 0$ <p>K1N0</p>	K1 K1 N1	3

NO	PENYELESAIAN	SUB	JUMLAH
11 a) (i)	$\frac{6!}{2!} = 360$ atau setara ; $\frac{^6P_6}{2!} / \frac{^6C_6 \times 6!}{2!}$	N1	1
11 a) (ii)	$5! = 120$ atau $\frac{5! \times 2!}{2!} = 120$	N1	1
11 b)	<p><u>Pusingan 1:</u> Iriz &amp; Saga [Assuming]  <math>= 2C1 \times 1C1 \times 6C2 \times 6C3 \times 3C3 = 600</math> &amp; Tukar Kereta = 1 cara  NOTA:  <math>2C1</math> = Pilih pemandu untuk kereta 1  <math>1C1</math> = Pilih pemandu untuk kereta 2  <math>6C2</math> = Pilih dua kereta daripada 6 kereta  <math>6C3</math> = Pilih 3 penumpang daripada 6 penumpang untuk kereta 1  <math>3C3</math> = Pilih 3 penumpang daripada 3 penumpang untuk kereta 2</p> <p><u>Pusingan 2:</u> x50 &amp; x70 [Assuming]  <math>= 2C1 \times 1C1 \times 4C2 \times 6C3 \times 3C3 = 240</math> &amp; Tukar Kereta = 1 cara  NOTA:  <math>2C1</math> = Pilih pemandu untuk kereta 1  <math>1C1</math> = Pilih pemandu untuk kereta 2  <math>4C2</math> = Pilih dua kereta daripada 4 kereta  <math>6C3</math> = Pilih 3 penumpang daripada 6 penumpang untuk kereta 1  <math>3C3</math> = Pilih 3 penumpang daripada 3 penumpang untuk kereta 2</p> <p><u>Pusingan 3:</u> Persona &amp; Exora [Assuming]  <math>= 2C1 \times 1C1 \times 2C2 \times 6C3 \times 3C3 = 40</math> &amp; Tukar Kereta = 1 cara  NOTA:  <math>2C1</math> = Pilih pemandu untuk kereta 1  <math>1C1</math> = Pilih pemandu untuk kereta 2  <math>2C2</math> = Pilih dua kereta daripada 2 kereta  <math>6C3</math> = Pilih 3 penumpang daripada 6 penumpang untuk kereta 1  <math>3C3</math> = Pilih 3 penumpang daripada 3 penumpang untuk kereta 2  Mana-mana satu kiraan di atas betul atau setara [1 m]  Bilangan Cara = <math>600(1) + 240(1) + 40(1)</math> [1 m]  = 880 [1 m]</p>	3	7
11 c)	$2! =$ Susun x50 dan x70 bersebelahan $(5-1)! =$ Susun keenam-enam model dalam bulatan Bilangan susunan berbeza $= 2!(5-1)!$ atau $\frac{5!}{5} \times 2!$ = 48	K1 N1	2

NO	PENYELESAIAN	SUB	JUMLAH
12 a)	 <ul style="list-style-type: none"> <li>• Garis lurus dan paksi dilukis menggunakan pembaris/alat tepi lurus.</li> <li>• Semua koordinat betul dan tajuk paksi betul.</li> <li>• Abaikan pintasan-Y</li> </ul>	1	4
12 b)	$y^2 = p\sqrt{x} - 8 \quad \text{P1}$ $p = \frac{16-4}{16-8}$ $p = * \frac{3}{2} / 1.5 \quad \text{K1}$ $y^2 = \frac{3}{2}\sqrt{x} - 8 \quad \text{N1 [terima } Y = \frac{3}{2}X - 8]$ <p>[terima murid menjawab (b) dahulu kemudian (a)]</p>	3	

NO	PENYELESAIAN	SUB	JUMLAH
13 a)	$f(x) = -\frac{3}{100} \left[ x^2 - \frac{20}{3}x - \frac{325}{3} \right]$ $f(x) = -\frac{3}{100} \left[ x^2 - \frac{20}{3}x + \left( \frac{-20}{3} \right)^2 - \left( \frac{-20}{3} \right)^2 - \frac{325}{3} \right] \quad \text{K1}$ $f(x) = -\frac{3}{100} \left[ \left( x - \frac{10}{3} \right)^2 - \frac{1075}{9} \right]$ $f(x) = -\frac{3}{100} \left( x - \frac{10}{3} \right)^2 + \frac{43}{12} \quad \text{N1}$ <p>setara <math>f(x) = -0.03 \left( x - \frac{10}{3} \right)^2 + \frac{43}{12}</math></p> <p>Tinggi maksimum = <math>\frac{43}{12}</math> @ <math>3\frac{7}{12}</math> @ 3.583 <math>\quad \text{N1}</math></p> <p>*K0 jika <math>\left( \frac{-20}{3} \right)^2 - \left( \frac{-20}{3} \right)^2</math> tidak dilihat</p> <p>Terima guna <math>f'(x)</math></p>	3	8

13 b)	$f(9) = -\frac{3}{100}(9)^2 + \frac{1}{5}(9) + \frac{13}{4}$ $= 2.62$ <p>Tinggi bola di atas jaring</p> $= 2.62 - 2.43$ $= 0.19$	K1 N1	2
13 c)	$x = \frac{-\left(\frac{1}{5}\right) \pm \sqrt{\left(\frac{1}{5}\right)^2 - 4\left(-\frac{3}{100}\right)\left(\frac{13}{4}\right)}}{2\left(-\frac{3}{100}\right)}$ $x = 14.262, x = -7.596$ [Diabaikan] <p>Ya, kerana jarak bola mencecah lantai = <math>14.262 &lt; 18</math></p> <p>*Mesti guna FORMULA</p>	K1	2
13 d)	<p>(*) Graf mesti melengkung</p> <ul style="list-style-type: none"> <li>• Titik 3.25 mesti lebih rendah dari titik maksimum.</li> <li>• 14.262 wajib tulis</li> </ul>		1

<b>NO</b>	<b>PENYELESAIAN</b>	<b>SUB</b>	<b>JUMLAH</b>
14 a)	<p>Adib [9 bahagian]</p> $S_9 = 213.36$ $\frac{9}{2} [2k + (9-1)h] = 213.36 \quad \text{K1 } (@ \quad \frac{16}{2} [2k + (16-1)h])$ $9k + 36h = 213.36 \quad \dots(1)$ <p>Azim [16 bahagian]</p> $S_{16} = 304.80$ $\frac{16}{2} [2k + (16-1)h] = 304.80$ $2k + 15h = 38.10 \quad \dots(2)$ $(1) \times 2 : 18k + 72h = 426.72 \quad \dots(3)$ $(2) \times 9 : 18k + 135h = 342.90 \quad \dots(4)$ $(4) - (3) : 63h = -83.82$ $h = -1.33$ <p>Ganti <math>h = -1.33</math> dalam (1)</p> $9k + 36(-1.33) = 213.36 \quad \text{K1}$ $k = 29.03$ <p>Alternatif: Ganti <math>h = -1.33</math> dalam (2)</p> $2k + 15(-1.33) = 38.10$ $k = 29.03$ $\therefore h = -1.33, k = 29.03 \quad \text{N1N1}$	4	8
14 b)	$T_n = 15.73$ $29.03 + (n-1)(-1.33) = 15.73 \quad \text{K1}$ $30.36 - 1.33n = 15.73$ $n = 11 \quad \text{N1}$ $S_{11} = \frac{11}{2} [2(29.03) + (11-1)(-1.33)] \quad \text{K1}$ <p>@</p> $S_{11} = \frac{11}{2} [29.03 + 15.73]$ $S_{11} = 246.18$ $\therefore \text{Julat ketinggian Aiman ialah } 147.32 - 160.02 \text{ cm} \quad \text{N1}$	4	

NO	PENYELESAIAN	MARKAH
15. (a)	$6x = 10x - 4 \quad \text{K1}$ $x = 1$ $y = 6(1) @ y = 10(1) - 4$ $(1, 6) \quad \text{N1}$	2
15. b)	<p style="text-align: center;"><b>ALTERNATIF A</b></p> $6x = 10x - 4 \quad \text{K1}$ $x = 1$ <p>Bila <math>x = 1 \rightarrow y = 6(1) = 6</math>, Bila <math>y = 0 \rightarrow 0 = 10x - 4</math></p> $x = \frac{2}{5} @ 0.4$ $y = 6x + x^2 \text{ dilihat} \quad \text{K1}$ $\text{Area} = \left  \int_{-6}^0 (6x + x^2) dx \right  + \frac{1}{2}(1)(6) - \frac{1}{2}(6)\left(1 - \frac{2}{5}\right) \quad \text{K1 kamiran}$ <p style="color: red; text-align: right;">[abaikan tanda mutlak]</p> $= \left  \left[ \frac{6x^2}{2} + \frac{x^3}{3} \right]_{-6}^0 \right  + (3 - 1.8) \quad \text{K1 jumlah luas}$ $= \left[ \left( \frac{6(0)^2}{2} + \frac{0^3}{3} \right) - \left( \frac{6(-6)^2}{2} + \frac{(-6)^3}{3} \right) \right] + 1.2 \quad \text{K1 ganti nilai}$ $=  -36  + 1.2$ $= 37 \frac{1}{5} \text{ unit}^2 / \frac{186}{5} \text{ unit}^2 / 37.2 \text{ unit}^2 \quad \text{N1}$ <p style="color: red; text-align: right;">[N0 jika abaikan tanda mutlak]</p> <p style="text-align: right;">6</p> <p style="text-align: center;"><b>ALTERNATIF B</b></p> $6x = 10x - 4 \quad \text{K1}$ $x = 1$ $y = 6x + x^2 \text{ dilihat} \quad \text{K1}$ $\left  \left[ \frac{6x^2}{2} + \frac{x^3}{3} \right]_{-6}^0 \right  \quad \text{K1 kamiran betul}$ $\left  \left[ \frac{6x^2}{2} + \frac{x^3}{3} \right]_{-6}^0 \right  - \left( \left[ \frac{6x^2}{2} \right]_0^1 - \left[ \frac{10x^2}{2} - 4x \right]_{\frac{2}{5}}^1 \right) \quad \text{K1 kamiran dan ganti had dengan betul}$ $\left  \left[ \frac{6(0)^2}{2} + \frac{(0)^3}{3} \right] - \left[ \frac{6(-6)^2}{2} + \frac{(-6)^3}{3} \right] \right  \quad \text{K1 ganti nilai}$	

$$\begin{aligned}
 & \text{Atau} \left[ \left( \frac{6(1)^2}{2} - \frac{6(0)^2}{2} \right) - \left( \frac{10(1)^2}{2} - 4(1) \right) - \left( \frac{10\left(\frac{2}{5}\right)^2}{2} - 4\left(\frac{2}{5}\right) \right) \right] \\
 & 36 + \left( 3 - \frac{9}{5} \right) \\
 & = 37 \frac{1}{5} \text{ unit}^2 / \frac{186}{5} \text{ unit}^2 / 37.2 \text{ unit}^2
 \end{aligned}$$

N1

JUMLAH

**8**

### PERATURAN PERMARKAHAN TAMAT